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SUB.: MATHS (NCERT BASED)

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Chapter 4:- Quadratic Equations

Methods to solve the Quadratic Equations

There are three methods to solve the Quadratic Equations-

1. Factorisation Method

In this method, we factorise the equation into two linear factors and equate each factor to zero to find the roots of the given equation.

Step 1: Given Quadratic Equation in the form of $ax^2 + bx + c = 0$.

Step 2: Split the middle term bx as $mx + nx$ so that the sum of m and n is equal to b and the product of m and n is equal to ac .

Step 3: By factorization we get the two linear factors $(x + p)$ and $(x + q)$

$$ax^2 + bx + c = 0 = (x + p)(x + q) = 0$$

Step 4: Now we have to equate each factor to zero to find the value of x .

$$x^2 - 2x - 15 = 0$$

$$(x + 3)(x - 5) = 0$$

$$x + 3 = 0 \text{ or } x - 5 = 0$$

$$x = -3 \text{ or } x = 5$$

$$x = \{-3, 5\}$$

These values of x are the two roots of the given Quadratic Equation.

2. Completing the square method

In this method, we convert the equation in the square form $(x + a)^2 - b^2 = 0$ to find the roots.

Step 1: Given Quadratic Equation in the standard form $ax^2 + bx + c = 0$.

Step 2: Divide both sides by a

$$x^2 + \frac{b}{a}x + \frac{c}{a} = 0$$

Step 3: Transfer the constant on RHS then add square of the half of the coefficient of x $\left(\frac{b}{2a}\right)^2$ i.e. on both sides

$$x^2 + \frac{b}{a}x = -\frac{c}{a}$$

$$x^2 + 2\left(\frac{b}{2a}\right)x + \left(\frac{b}{2a}\right)^2 = -\frac{c}{a} + \left(\frac{b}{2a}\right)^2$$

Step 4: Now write LHS as perfect square and simplify the RHS.

$$\left(x + \frac{b}{2a}\right)^2 = \frac{b^2 - 4ac}{4a^2}$$

Step 5: Take the square root on both the sides.

$$x + \frac{b}{2a} = \pm \sqrt{\frac{b^2 - 4ac}{4a^2}}$$

Step 6: Now shift all the constant terms to the RHS and we can calculate the value of x as there is no variable at the RHS.

$$x = \pm \sqrt{\frac{b^2 - 4ac}{4a^2}} - \frac{b}{2a}$$

3. Quadratic formula method

In this method, we can find the roots by using quadratic formula. The quadratic formula is

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

where a, b and c are the real numbers and $b^2 - 4ac$ is called discriminant.

To find the roots of the equation, put the value of a, b and c in the quadratic formula.

Nature of Roots

From the quadratic formula, we can see that the two roots of the Quadratic Equation are

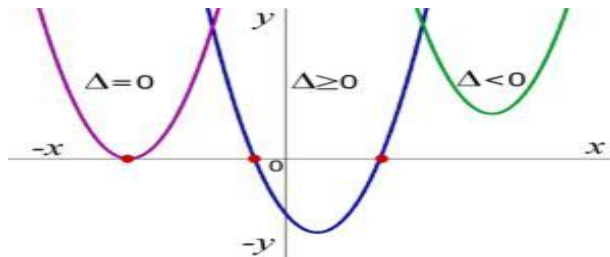
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$$x = \frac{-b + \sqrt{b^2 - 4ac}}{2a} \text{ and } \frac{-b - \sqrt{b^2 - 4ac}}{2a}$$

$$\text{or } x = \frac{-b \pm \sqrt{D}}{2a}$$

Where $D = b^2 - 4ac$

The nature of the roots of the equation depends upon the value of D, so it is called the **discriminant**.



Value of discriminant	No. of roots	Value of roots
$D > 0$	Two distinct real roots	$\frac{-b + \sqrt{D}}{2a}, \frac{-b - \sqrt{D}}{2a}$
$D = 0$	Two equal and real roots	$-\frac{b}{2a}, -\frac{b}{2a}$
$D < 0$	No real roots	Nil